

Sixth Grade Math Curriculum

Course Description The goal of this course is to build on students' past knowledge to develop, understand, and demonstrate math concepts as they prepare for future programs in the middle school. Students will master concepts including, but not limited to, the number system, operations with rational numbers, solving one-step equations and inequalities, rates, ratios, and proportional reasoning. They will also explore geometry via area and volume, and explore statistics and probability.	Topics at a Glance Number Theory Integers Properties Solving Equations Linear Equations
Assessments • Summative and formative grade level assessments • Classroom assessments • Standardized Tests Grade Level Expectations Quantities can be expressed and compared using ratios and rates Formulate, represent, and use algorithms with positive rational numbers with flexibility, accuracy, and efficiency In the real number system, rational numbers have a unique location on the number line and in space Algebraic expressions can be used to generalize properties of arithmetic Variables are used to represent unknown quantities within equations and inequalities Visual displays and summary statistics of one-variable data condense the information in data sets into usable knowledge Objects in space and their parts and attributes can be measured and analyzed	 Effective Components Make sense of problems and persevere in solving them. Reason abstractly and quantitatively. Construct viable arguments and critique the reasoning of others. Model with mathematics. Use appropriate tools strategically Attend to precision. Look for and make use of structure. Look for and express regularity in repeated reasoning.

6th Grade Math Overview

1. Number Sense, Properties, and Operations

Number sense provides students with a firm foundation in mathematics. Students build a deep understanding of quantity, ways of representing numbers, relationships among numbers, and number systems. Students learn that numbers are governed by properties, and understanding these properties leads to fluency with operations.

Valwood Graduate Competencies

The Valwood graduate competencies are the preschool through twelfth-grade concepts and skills that all graduates will be able to demonstrate.

Valwood Graduate Competencies in the Number Sense, Properties, and Operations Standard are:

- > Understand the structure and properties of our number system. At their most basic level numbers are abstract symbols that represent real-world quantities
- Understand quantity through estimation, precision, order of magnitude, and comparison. The reasonableness of answers relies on the ability to judge appropriateness, compare, estimate, and analyze error
- Are fluent with basic numerical and symbolic facts and algorithms, and are able to select and use appropriate (mental math, paper and pencil, and technology) methods based on an understanding of their efficiency, precision, and transparency
- Make both relative (multiplicative) and absolute (arithmetic) comparisons between quantities. Multiplicative thinking underlies proportional reasoning
- Understand that equivalence is a foundation of mathematics represented in numbers, shapes, measures, expressions, and equations
- > Apply transformation to numbers, shapes, functional representations, and data

Content	Area: Mathematics - Sixth Grade	
Standard: 1. Number Sense, Properties, and Operations		
Valwood	d Graduates: both relative (multiplicative) and absolute (arithmetic) cor	mparisons between quantities. Multiplicative thinking underlies proportional
	LEVEL EXPECTATION	
Concept	ts and skills students master:	
1. Q	uantities can be expressed and compared using ratios and	rates.
	Evidence Outcomes	21 st Century Skills and Readiness Competencies
a rati b. Apply with relati c. Use ra mathema i.	the concept of a ratio and use ratio language to describe io relationship between two quantities. ¹ the concept of a unit rate a/b associated with a ratio a:b b ≠ 0, and use rate language in the context of a ratio ionship. ² atio and rate reasoning to solve real-world and atical problems. ³ Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.	 Inquiry Questions: How are ratios different from fractions? What is the difference between quantity and number? Relevance and Application: Knowledge of ratios and rates allows sound decision-making in daily life such as determining best values when shopping, creating mixtures, adjusting recipes, calculating car mileage, using speed to determine travel time, or making saving and investing decisions. Ratios and rates are used to solve important problems in science, business, and politics. For example developing more fuel-efficient vehicles, understanding voter registration and voter turnout in elections, or finding more cost-effective suppliers. Rates and ratios are used in mechanical devices such as bicycle gears, car transmissions, and clocks.
iii. iv. v. vi.	Solve unit rate problems including those involving unit pricing and constant speed. ⁴ Find a percent of a quantity as a rate per 100. ⁵ Solve problems involving finding the whole, given a part and the percent. Use common fractions and percents to calculate parts of whole numbers in problem situations including	 Nature of Discipline: 1. Mathematicians develop simple procedures to express complex mathematical concepts. 2. Mathematicians make sense of problems and persevere in solving them. 3. Mathematicians reason abstractly and quantitatively.
vii. viii.	comparisons of savings rates at different financial institutions. Express the comparison of two whole number quantities using differences, part-to-part ratios, and part-to-whole ratios in real contexts, including investing and saving Use ratio reasoning to convert measurement units. ⁶	 ¹ For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes." ² For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is 3/4 cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger." ³ e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. ⁴ For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed? ⁵ e.g., 30% of a quantity means 30/100 times the quantity.

Content Area: Mathematics - Sixth Grade		
Standard: 1. Number Sense, Properties, and Operations		
Valwood Graduates:		
	s, and are able to select and use appropriate (mental math, paper and	
pencil, and technology) methods based on an understanding of th	eir efficiency, precision, and transparency.	
GRADE LEVEL EXPECTATION		
Concepts and skills students master:		
Formulate, represent, and use algorithms with positive rational	numbers with flexibility, accuracy, and efficiency.	
Evidence Outcomes	21 st Century Skills and Readiness Competencies	
Students can:	Inquiry Questions:	
a. Fluently divide multi-digit numbers using standard algorithms.	1. Why might estimation be better than an exact answer?	
b. Fluently add, subtract, multiply, and divide multi-digit decimals	2. How do operations with fractions and decimals compare to	
using standard algorithms for each operation.	operations with whole numbers?	
c. Find the greatest common factor of two whole numbers less than	Relevance and Application:	
or equal to 100.	1. Rational numbers are an essential component of mathematics.	
d. Find the least common multiple of two whole numbers less than	Understanding fractions, decimals, and percentages is the basis	
or equal to 12.	for probability, proportions, measurement, money, algebra, and	
e. Use the distributive property to express a sum of two whole	geometry.	
numbers 1–100 with a common factor as a multiple of a sum of	Nature of Discipline:	
two whole numbers with no common factor. ⁷	1. Mathematicians envision and test strategies for solving problems.	
f. Interpret and model quotients of fractions through the creation of	2. Mathematicians model with mathematics.	
story contexts. ⁸	3. Mathematicians look for and make use of structure.	
g. Compute quotients of fractions. ⁹		
h. Solve word problems involving division of fractions by fractions,	⁷ For example, express 36 + 8 as 4 (9 + 2). ⁸ For example, create a story context for $(2/2) + (2/4)$ and use a visual fraction model.	
e.g., by using visual fraction models and equations to represent	⁸ For example, create a story context for $(2/3) \div (3/4)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to	
the problem. ¹⁰	explain that $(2/3) \div (3/4) = 8/9$ because 3/4 of 8/9 is 2/3.	
	⁹ In general, $(a/b) \div (c/d) = ad/bc.$).	
	¹⁰ How much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 3/4-cup servings are in 2/3 of a cup of yogurt? How wide is a	
	rectangular strip of land with length 3/4 mi and area 1/2 square mi?	

Content Area: Mathematics - Sixth Grade		
Standard: 1. Number Sense, Properties, and Operations		
Valwood Graduates:		
Understand the structure and properties of our number system. At their n	nost basic level numbers are abstract symbols that represent	
real-world quantities.		
GRADE LEVEL EXPECTATION		
Concepts and skills students master:		
3. In the real number system, rational numbers have a unique location or	·	
Evidence Outcomes	21 st Century Skills and Readiness Competencies	
 Students can: a. Explain why positive and negative numbers are used together to describe quantities having opposite directions or values.¹¹ i. Use positive and negative numbers to represent quantities in use positive and negative numbers to represent quantities. 	Inquiry Questions: 1. Why are there negative numbers? 2. How do we compare and contrast numbers? 3. Are there more rational numbers than integers?	
 real-world contexts, explaining the meaning of 0 in each situation. b. Use number line diagrams and coordinate axes to represent points on the line and in the plane with negative number coordinates.¹² Describe a rational number as a point on the number line. Use opposite signs of numbers to indicate locations on opposite sides of 0 on the number line. ii. Identify that the opposite of the opposite of a number is the number itself.¹³ iv. Explain when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes. v. Find and position integers and other rational numbers on a horizontal or vertical number line diagram. vi. Find and position pairs of integers and other rational numbers on a coordinate plane. c. Order and find absolute value of rational numbers. i. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram.¹⁴ write, interpret, and explain statements of order for rational numbers in real-world contexts.¹⁵ 	 Relevance and Application: Communication and collaboration with others is more efficient and accurate using rational numbers. For example, negotiating the price of an automobile, sharing results of a scientific experiment with the public, and planning a party with friends. Negative numbers can be used to represent quantities less than zero or quantities with an associated direction such as debt, elevations below sea level, low temperatures, moving backward in time, or an object slowing down. Nature of Discipline: Mathematicians use their understanding of relationships among numbers and the rules of number systems to create models of a wide variety of situations. Mathematicians construct viable arguments and critique the reasoning of others. Mathematicians attend to precision. ¹¹ e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge). ¹² Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane. ¹³ e.g., -(-3) = 3, and that 0 is its own opposite. ¹⁴ For example, interpret -3 > -7 °C to express the fact that -3 °C is warmer than -7 °C. 	

	III.	Situation. ¹⁰	¹⁶ For example, for an account balance of -30 dollars, write $ -30 = 30$ to describe the size of the debt in dollars. ¹⁷ For example, recognize that an account balance less than -30 dollars represents a debt greater than 30 dollars.
	iv.	Distinguish comparisons of absolute value from statements about order. ¹⁷	
d. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane including the use of coordinates and absolute value to find distances between points with		r quadrants of the coordinate plane including the use of	
		me first coordinate or the same second coordinate.	

2. Patterns, Functions, and Algebraic Structures

Pattern sense gives students a lens with which to understand trends and commonalities. Being a student of mathematics involves recognizing and representing mathematical relationships and analyzing change. Students learn that the structures of algebra allow complex ideas to be expressed succinctly.

Valwood Graduate Competencies

The Valwood graduate competencies are the preschool through twelfth-grade concepts and skills that all graduates will be able to demonstrate.

Valwood Graduate Competencies in the 2. Patterns, Functions, and Algebraic Structures Standard are:			
\checkmark	Are fluent with basic numerical and symbolic facts and algorithms, and are able to select and use appropriate (mental math, paper and pencil, and technology) methods based on an understanding of their efficiency, precision, and transparency		
\checkmark	Understand that equivalence is a foundation of mathematics represented in numbers, shapes, measures, expressions, and equations		
	Make sound predictions and generalizations based on patterns and relationships that arise from numbers, shapes, symbols, and data		
\mathbf{A}	Make claims about relationships among numbers, shapes, symbols, and data and defend those claims by relying on the properties that are the structure of mathematics		
A	Use critical thinking to recognize problematic aspects of situations, create mathematical models, and present and defend solutions		

Content Area: Mathematics - Sixth Grade		
Standard: 2. Patterns, Functions, and Algebraic Structures		
Valwood Graduates:		
	ls, and data and defend those claims by relying on the properties that are	
the structure of mathematics.		
GRADE LEVEL EXPECTATION		
Concepts and skills students master:		
1. Algebraic expressions can be used to generalize properties of a	arithmetic.	
Evidence Outcomes	21 st Century Skills and Readiness Competencies	
Students can: a. Write and evaluate numerical expressions involving whole-	Inquiry Questions: 1. If we didn't have variables, what would we use?	
number exponents.	2. What purposes do variable expressions serve?	
b. Write, read, and evaluate expressions in which letters stand	3. What are some advantages to being able to describe a pattern	
for numbers.	using variables?	
i. Write expressions that record operations with	4. Why does the order of operations exist?	
numbers and with letters standing for numbers. ¹	5. What other tasks/processes require the use of a strict order of	
ii. Identify parts of an expression using mathematical	steps?	
terms (sum, term, product, factor, quotient,	Relevance and Application:	
coefficient) and describe one or more parts of an	1. The simplification of algebraic expressions allows one to	
expression as a single entity. ²	communicate mathematics efficiently for use in a variety of	
iii. Evaluate expressions at specific values of their	contexts.	
variables including expressions that arise from formulas used in real-world problems. ³	2. Using algebraic expressions we can efficiently expand and	
iv. Perform arithmetic operations, including those	describe patterns in spreadsheets or other technologies.	
involving whole-number exponents, in the	Nature of Discipline: 1. Mathematicians use place value to represent many numbers with	
conventional order when there are no parentheses to	only ten digits.	
specify a particular order (Order of Operations).	2. Mathematicians construct viable arguments and critique the	
c. Apply the properties of operations to generate equivalent	reasoning of others.	
expressions. ⁴	3. Mathematicians look for and make use of structure.	
d. Identify when two expressions are equivalent. ⁵	4. Mathematicians look for and express regularity in repeated	
	reasoning.	
	¹ For example, express the calculation "Subtract y from 5" as $5 - y$. ² For example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7)	
	as both a single entity and a sum of two terms.	
	3 For example, use the formulas V=s3 and A=6s2 to find the volume and surface area of a	
	cube with sides of length s = $1/2$. ⁴ For example, apply the distributive property to the expression 3 (2 + x) to produce the	
	equivalent expression 6 + $3x$; apply the distributive property to the expression 3 (2 + x) to produce the	
	to produce the equivalent expression 6 $(4x + 3y)$; apply properties of operations to $y + y$	
	 + y to produce the equivalent expression 3y. ⁵ i.e., when the two expressions name the same number regardless of which value is 	
	substituted into them). For example, the expressions $y + y + y$ and $3y$ are equivalent	
	because they name the same number regardless of which number y stands for. Reason	
	about and solve one-variable equations and inequalities.	

Content Area: Mathematics - Sixth Grade

Standard: 2. Patterns, Functions, and Algebraic Structures

Valwood Graduates:

Make claims about relationships among numbers, shapes, symbols, and data and defend those claims by relying on the properties that are the structure of mathematics.

GRADE LEVEL EXPECTATION

Concepts and skills students master:

2. Variables are used to represent unknown quantities within equations and inequalities.

	Evidence Outcomes	21 st Century Skills and Readiness Competencies
	ents can: Describe solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true?	Inquiry Questions:1. Do all equations have exactly one unique solution? Why?2. How can you determine if a variable is independent or dependent?
b.	Use substitution to determine whether a given number in a	Relevance and Application:
C.	 specified set makes an equation or inequality true. Use variables to represent numbers and write expressions when solving a real-world or mathematical problem. i. Recognize that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set. 	 Variables allow communication of big ideas with very few symbols. For example, d=r×t is a simple way of showing the relationship between the distance one travels and the rate of speed and time traveled, and C=nd expresses the relationship between circumference and diameter of a circle. Variables show what parts of an expression may change
d.	Solve real-world and mathematical problems by writing and solving equations of the form $x + p = q$ and $px = q$ for cases in which p, q and x are all nonnegative rational numbers.	compared to those parts that are fixed or constant. For example, the price of an item may be fixed in an expression, but the number of items purchased may change.
e.	Write an inequality of the form $x > c$ or $x < c$ to represent a constraint or condition in a real-world or mathematical problem.	Nature of Discipline: 1. Mathematicians use graphs and equations to represent relationships among variables. They use multiple
f.	Show that inequalities of the form $x > c$ or $x < c$ have infinitely many solutions; represent solutions of such inequalities on number line diagrams.	 representations to gain insights into the relationships between variables. 2. Mathematicians can think both forward and backward through a problem. An equation is like the end of a story about what happened to a variable. By reading the story backward, and undoing each step, mathematicians can find the value of the variable. 3. Mathematicians model with mathematics.
		⁶ For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation $d = 65t$ to represent the relationship between distance and time.

g.		esent and analyze quantitative relationships between ndent and independent variables. Use variables to represent two quantities in a real- world problem that change in relationship to one another.
	ii.	Write an equation to express one quantity, thought of as the dependent variable, in terms of the other
	iii.	quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. ⁶

3. Data Analysis, Statistics, and Probability

Data and probability sense provides students with tools to understand information and uncertainty. Students ask questions and gather and use data to answer them. Students use a variety of data analysis and statistics strategies to analyze, develop and evaluate inferences based on data. Probability provides the foundation for collecting, describing, and interpreting data.

Valwood Graduates

The Valwood graduate competencies are the preschool through twelfth-grade concepts and skills that all students who complete the Valwood education system must master to ensure their success in a postsecondary and workforce setting.

Valwood Graduate Competencies in the 3. Data Analysis, Statistics, and Probability Standard are:

- Recognize and make sense of the many ways that variability, chance, and randomness appear in a variety of contexts
- Solve problems and make decisions that depend on understanding, explaining, and quantifying the variability in data
- > Communicate effective logical arguments using mathematical justification and proof. Mathematical argumentation involves making and testing conjectures, drawing valid conclusions, and justifying thinking
- > Use critical thinking to recognize problematic aspects of situations, create mathematical models, and present and defend solutions

Content Area: Mathematics - Sixth Grade		
Standard: 3. Data Analysis, Statistics, and Probability		
Valwood Graduates:		
Solve problems and make decisions that depend on understanding, e	explaining, and quantifying the variability in data.	
GRADE LEVEL EXPECTATION		
Concepts and skills students master:		
1. Visual displays and summary statistics of one-variable data conde		
Evidence Outcomes	21 st Century Skills and Readiness Competencies	
 Students can: a. Identify a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers.¹ b. Demonstrate that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape. c. Explain that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number. d. Summarize and describe distributions. i. Display numerical data in plots on a number line, including dot plots, histograms, and box plots. ii. Summarize numerical data sets in relation to their context. 1. Report the number of observations. 2. Describe the nature of the attribute under investigation, including how it was measured and its units of measurement. 	 Inquiry Questions: Why are there so many ways to describe data? When is one data display better than another? When is one statistical measure better than another? What makes a good statistical question? Relevance and Application: Comprehension of how to analyze and interpret data allows better understanding of large and complex systems such as analyzing employment data to better understand our economy, or analyzing achievement data to better understand our economy, or analyzing achievement data to better understand our education system. Different data analysis tools enable the efficient communication of large amounts of information such as listing all the student scores on a state test versus using a box plot to show the distribution of the scores. Nature of Discipline: Mathematicians leverage strategic displays to reveal data. Mathematicians use appropriate tools strategically. Mathematicians attend to precision. 	
 mean) and variability (interqualitie range and/of mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered. 4. Relate the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered. 	¹ For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages.	

4. Shape, Dimension, and Geometric Relationships

Geometric sense allows students to comprehend space and shape. Students analyze the characteristics and relationships of shapes and structures, engage in logical reasoning, and use tools and techniques to determine measurement. Students learn that geometry and measurement are useful in representing and solving problems in the real world as well as in mathematics.

Valwood Graduate Competencies

The Valwood graduate competencies are the preschool through twelfth-grade concepts and skills that all graduates will be able to demonstrate.

Valwood Graduate Competencies in the 4. Shape, Dimension, and Geometric Relationships standard are:

- Understand quantity through estimation, precision, order of magnitude, and comparison. The reasonableness of answers relies on the ability to judge appropriateness, compare, estimate, and analyze error
- Make sound predictions and generalizations based on patterns and relationships that arise from numbers, shapes, symbols, and data
- > Apply transformation to numbers, shapes, functional representations, and data
- Make claims about relationships among numbers, shapes, symbols, and data and defend those claims by relying on the properties that are the structure of mathematics
- Use critical thinking to recognize problematic aspects of situations, create mathematical models, and present and defend solutions

Content Area: Math - Sixth Grade		
Standard: 4. Shape, Dimension, and Geometric Relationships		
Valwood Graduates:		
Make claims about relationships among numbers, shapes, symbols, ar	nd data and defend those claims by relying on the properties that are	
the structure of mathematics.		
GRADE LEVEL EXPECTATION		
Concepts and skills students master:		
1. Objects in space and their parts and attributes can be measured an		
Evidence Outcomes	21 st Century Skills and Readiness Competencies	
 Students can: a. Develop and apply formulas and procedures for area of plane figures Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes. Apply these techniques in the context of solving real-world 	 Inquiry Questions: Can two shapes have the same volume but different surface areas? Why? Can two figures have the same surface area but different volumes? Why? What does area tell you about a figure? What properties affect the area of figures? 	
 and mathematical problems. b. Develop and apply formulas and procedures for volume of regular prisms. Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths. Show that volume is the same as multiplying the edge lengths of a rectangular prism. Apply the formulas V = I w h and V = b h to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems. Draw polygons in the coordinate plane given coordinates for the vertices. Use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Develop and apply formulas and procedures for the surface area. Represent three-dimensional figures using nets made up of rectangles and triangles. Use nets to find the surface area of figures. Apply techniques for finding surface area in the context of solving real-world and mathematical problems. 	 Relevance and Application: 1. Knowledge of how to find the areas of different shapes helps do projects in the home and community. For example how to use the correct amount of fertilizer in a garden, buy the correct amount of paint, or buy the right amount of material for a construction project. 2. The application of area measurement of different shapes aids with everyday tasks such as buying carpeting, determining watershed by a center pivot irrigation system, finding the number of gallons of paint needed to paint a room, decomposing a floor plan, or designing landscapes. Nature of Discipline: 1. Mathematicians realize that measurement always involves a certain degree of error. 2. Mathematicians make sense of problems and persevere in solving them. 4. Mathematicians reason abstractly and quantitatively. 	